

Atomic data for neutron-capture elements

I. Photoionization and recombination properties of low-charge selenium ions

N. C. Sterling¹★ and Michael C. Witthoeft²

¹ Michigan State University, Department of Physics and Astronomy, 3248 Biomedical Physical Sciences, East Lansing, MI, 48824-2320, USA, e-mail: sterling@pa.msu.edu

² NASA Goddard Space Flight Center, Code 662, Greenbelt, MD 20771, USA, e-mail: michael.c.witthoeft@nasa.gov

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ABSTRACT

We present multi-configuration Breit-Pauli AUTOSTRUCTURE calculations of distorted-wave photoionization (PI) cross sections, and total and partial final-state resolved radiative recombination (RR) and dielectronic recombination (DR) rate coefficients for the first six ions of the trans-iron element Se. These calculations were motivated by the recent detection of Se emission lines in a large number of planetary nebulae. Se is a potentially useful tracer of neutron-capture nucleosynthesis, but accurate determinations of its abundance in photoionized nebulae have been hindered by the lack of atomic data governing its ionization balance. Our calculations were carried out in intermediate coupling with semi-relativistic radial wavefunctions. PI and recombination data were determined for levels within the ground configuration of each ion, and experimental PI cross-section measurements were used to benchmark our results. For DR, we allowed $\Delta n = 0$ core excitations, which are important at photoionized plasma temperatures. We find that DR is the dominant recombination process for each of these Se ions at temperatures representative of photoionized nebulae ($\sim 10^4$ K). In order to estimate the uncertainties of these data, we compared results from three different configuration-interaction expansions for each ion, and also tested the sensitivity of the results to the radial scaling factors in the structure calculations. We find that the internal uncertainties are typically 30–50% for the direct PI cross sections and $\sim 10\%$ for the computed RR rate coefficients, while those for low-temperature DR can be considerably larger (from 15–30% up to two orders of magnitude) due to the unknown energies of near-threshold autoionization resonances. These data are available at the CDS, and fitting coefficients to the total RR and DR rate coefficients are presented. The results are suitable for incorporation into photoionization codes used to numerically simulate astrophysical nebulae, and will enable robust determinations of nebular Se abundances.

Key words. atomic data - atomic processes - HII regions - nucleosynthesis, abundances - planetary nebulae: general - stars:evolution

1. Introduction

The abundances of neutron(n)-capture elements (atomic number $Z > 30$) are sensitive probes of the nucleosynthetic histories of stellar populations and the chemical evolution of the Universe (Wallerstein et al. 1997; Busso et al. 1999; Sneden et al. 2008). Our knowledge of the production of these elements is largely based on the interpretation of abundances derived from stellar spectroscopy (e.g., Smith & Lambert 1990; Busso et al. 1999; Travaglio et al. 2004; Sneden et al. 2008; Roederer et al. 2010, and references therein). However, only a limited number of trans-iron elements can be detected in stellar spectra. Moreover, some classes of stars or stages of evolution with high mass-loss rates are very difficult to study spectroscopically due to photospheric obscuration.

The recent detection of emission lines from n -capture elements in a large number of planetary nebulae (PNe) (Sterling et al. 2007; Sharpee et al. 2007; Sterling & Dinerstein 2008; Sterling et al. 2009), as well as other astrophysical objects including H II regions (e.g., Aspin 1994; Lumsden & Puxley 1996; Luhman et al. 1998; Baldwin et al. 2000; Puxley et al. 2000; Okumura et al. 2001; Blum & McGregor 2008; Roman-Lopes et al. 2009), starburst galaxies (Vanzi et al. 2008), and active galactic nuclei (Thompson et al. 1978), has demonstrated that nebular spectroscopy is a potentially

powerful tool for investigating the nucleosynthesis and chemical evolution of trans-iron species. The abundances of n -capture elements are of particular interest in PNe, since these species can be produced in PN progenitor stars via slow n -capture nucleosynthesis (the “ s -process”) during the asymptotic giant branch (AGB) stage of evolution.

Nebular spectroscopy provides access to many elements that cannot be detected in cool giant stars, such as the lightest n -capture elements ($Z = 31$ – 36) and noble gases. Due to the difficulty in detecting these species in stellar spectra or supernova remnants (Wallerstein et al. 1995), the origins of light n -capture elements are based predominantly on theoretical considerations that lack empirical validation. In addition, nebular spectroscopy enables investigations of nucleosynthesis in classes or evolutionary stages of stars obscured by optically thick circumstellar envelopes. For example, intermediate-mass AGB stars (4 – $8 M_{\odot}$) experience heavy mass loss, shielding their photospheres in a cocoon of circumstellar material that hinders spectroscopic investigations in the wavelength regimes of many useful n -capture element transitions. As a result, the contribution of these stars to the Galactic inventory of heavy element nuclei is poorly understood (e.g., Karakas et al. 2009). However, these intermediate-mass stars produce PNe in which n -capture element emission lines are readily detected (Sharpee et al. 2007; Sterling & Dinerstein 2008). Likewise, AGB stars that become carbon-rich as a result of convective dredge-up (see Busso et al. 1999) are char-

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acterized by high opacities (Marigo 2002) that substantially increase their mass-loss rates, and hence *s*-process enrichments engendered by the final stages of AGB evolution are not well-constrained. PNe are composed of material from the stellar envelope at the end of the AGB phase, and hence are useful probes of *s*-process enrichments during late AGB evolution.

However, the accuracy of nebular *n*-capture element abundances is hindered by the poorly known atomic data for these species, thereby limiting the usefulness of nebular spectroscopy for studying the origins of these elements. The reason for this is that generally only one or two ions of *n*-capture elements have been detected in individual nebulae, and hence the abundances of unobserved ions must be estimated in order to derive elemental abundances. This is most robustly achieved by numerically simulating the thermal and ionization structure of nebulae with photoionization codes such as Cloudy (Ferland et al. 1998), but the reliability of these models strongly depends on the availability of accurate atomic data for processes that control the ionization balance. For photoionized nebulae such as PNe, these data include photoionization (PI) cross sections and rate coefficients for radiative recombination (RR), dielectronic recombination (DR), and charge transfer (CT). Unfortunately, such data have not been determined for the vast majority of trans-iron element ions.

To address this need, we have computed multi-configuration Breit-Pauli (MCBP) distorted-wave PI cross sections and RR and DR rate coefficients for the first six Se ions, using the atomic structure code AUTOSTRUCTURE (Badnell 1986, 1997). Along with Kr and Xe, Se is one of the most widely observed *n*-capture elements in ionized nebulae (Sharpee et al. 2007; Sterling & Dinerstein 2008). In fact, Se has been identified in nearly twice as many PNe as any other trans-iron element, and hence is the initial target for our study. In subsequent papers, we will present similar data for low-charge Kr and Xe ions, as well as CT rate coefficients for several *n*-capture elements. These data will be suitable for incorporation into photoionization codes such as Cloudy, which can be used to robustly determine correction factors for the abundances of unobserved ions, enabling much more accurate abundance determinations of *n*-capture elements in ionized nebulae than previously possible.

Until our study, the photoionization and recombination properties of Se ions had received very little attention, aside from a handful of PI studies of neutral Se (Manson et al. 1979; Gibson et al. 1986; Chen & Robicheaux 1994), which is a trace species in ionized nebulae such as PNe. We therefore utilize recently conducted experimental PI cross-section measurements of Se ions (Esteves et al. 2009; Sterling et al. 2011; Esteves et al. 2010, 2011) as a comparison and benchmark to our calculations.

We estimate the uncertainties in our computed data by utilizing three different configuration-interaction (CI) expansions for each ion, and test the sensitivity of our results to various internal parameters of the AUTOSTRUCTURE code. Upon completion of our theoretical study of Se, Kr, and Xe ions we will use Monte Carlo simulations with photoionization codes to reveal the effects of these atomic data uncertainties on nebular abundance determinations, illustrating which systems and atomic processes require further theoretical and/or experimental analysis.

This paper is organized as follows: in Sect. 2, we provide details of our calculations, and in Sect. 3 we present our computed PI cross sections and RR and DR rate coefficients along with their associated uncertainties. Finally, in Sect. 4 we summarize our results and provide concluding remarks.

2. Calculations and methodology

We have computed the electronic structure and MCBP distorted-wave PI cross sections for Se⁰–Se⁵⁺ with the AUTOSTRUCTURE code (Badnell 1986, 1997). Higher charge states were not considered since they are negligibly populated in PNe, whose central stars are not sufficiently hot (generally $< 2 \times 10^5$ K; Napiwotzki 1999; Stanghellini et al. 2002) to significantly ionize species with ionization thresholds greater than 100 eV. RR and DR rate coefficients were determined from the direct and resonant portions of the PI cross sections, respectively, using detailed balance. We used the independent processes approximation (Pindzola et al. 1992) to treat RR and DR separately.

The theoretical background of such calculations have been provided elsewhere (Badnell et al. 2003; Badnell 2006b), and we refer the reader to those references for a full discussion. In each of the following subsections, we discuss details of calculations for each process considered.

2.1. Electronic structure

To test the sensitivity of our results to the adopted CI expansions, we constructed three different CI expansions for each Se ion (designated “small,” “medium,” and “large”). The medium configuration sets provide the best compromise between accuracy and computational expense, and are adopted as the basis for our PI, RR, and DR results. The CI expansions for each ion are listed in Table 1.¹

In all cases, the electronic structure was computed with Thomas-Fermi-Dirac-Amaldi model potentials, adopting intermediate-coupling and κ -averaged relativistic wavefunctions (Cowan & Griffin 1976). We Schmidt orthogonalized the κ -averaged orbitals in our calculations, but compared our PI and RR results with those obtained without forcing the radial orbitals to be orthogonal. The average of the LS term energies were optimized by varying the orbital radial scaling parameters so as to best reproduce experimental energy levels and ionization potentials from NIST (Ralchenko et al. 2008). The radial scaling parameters adopted for each CI expansion of each ion are given in Table 2. A comparison of selected calculated and experimental energies is shown in Table 3. We also compare our Einstein A-coefficients with those available in the literature in Table 4.

The structure computed with the medium configuration sets generally reproduce experimental energies and ionization potentials to a good degree of accuracy, lending credence to our use of orthogonalized radial orbitals. The ionization potentials are within 2–3% of the NIST values for all ions with the exception of Se⁰, which is a very challenging system to model but fortunately is negligibly populated in ionized nebulae such as PNe. The energies of most levels tabulated by NIST are reproduced to within 5% for Se⁺–Se⁶⁺, and to within 9% for the neutral case. A few exceptions occur, particularly for levels within the ground configuration, where the discrepancies with experiment are as large as 23% for Se⁺ 4s² 4p³ ²D_{3/2}.

The accuracies of the level energies affects those of the Einstein A-coefficients A_{ij} we computed. For forbidden transitions within the ground configurations, the main comparisons are the theoretical studies of Biémont & Hansen in the 1980s (see Table 4 for references), who utilized the Hartree-Fock with relativistic corrections (HFR) and Hartree-plus-statistical-exchange (HXR) methods. In many cases, our computed A_{ij} agree with

¹ Tables 1–4 are available in the online version of this article.

those previous studies to within 30–50%, but exceptions occur, particularly for the lowest-charge states. However, it is worth noting that our CI expansions generally are larger than those used by Biémont & Hansen, and hence include configuration mixing not incorporated in their calculations.

2.2. Photoionization

MCBP distorted-wave PI cross sections were computed in intermediate coupling for neutral Se and each of the first five ions. Cross sections were calculated for each level in the ground configurations, as the vast majority of ions in photoionized plasmas reside in the ground configuration. The CI expansions listed in Table 1 were used in these calculations, with radial scaling parameters from Table 2. In the cases of Se^+ , Se^{2+} , Se^{3+} , and Se^{5+} , experimental PI cross sections measured at the Advanced Light Source (ALS) synchrotron radiation facility at Lawrence Berkeley National Laboratory in California were used to test the accuracy of our computations (see Sect. 3.1.2).

PI cross sections were computed up to 100 Ryd for each ion. The length gauge was used at low energies, and AUTOSTRUCTURE automatically switched to velocity gauge at higher energies. Because of our use of κ -averaged relativistic orbitals, it was not possible to use acceleration gauge. The electron energy mesh was interpolated onto the photon energy mesh using a 4-point Lagrange interpolation. Photoexcitation-autoionization resonances were included for each system, over a more restricted energy range due to the finer energy mesh required for comparison to experimental measurements. In all cases, we utilized the radial scaling parameters associated with the $(N + 1)$ -electron ion, as tests showed that using the target scaling parameters led to very poor agreement with experimental PI cross sections. Scaling parameters for continuum orbitals were taken to be equal to those of the highest principal quantum number bound orbitals with the same orbital angular momentum for s , p , and d orbitals, and equal to unity otherwise.

2.3. Radiative recombination

Total and partial final-state resolved radiative recombination rate coefficients were computed from the direct PI cross sections using detailed balance. The CI expansions of the $(N + 1)$ -electron ions were augmented to include one-electron additions to the target's ground and mixing configurations. Since it was not possible to use acceleration gauge at high energies, the rate coefficients may be inaccurate at the highest temperatures. However, we have tested that this does not affect the accuracy at photoionized plasma temperatures (see Sect. 3.2.1). The rate coefficients were determined over the temperature range $(10^1 - 10^7)z^2$ K, where z is the charge. We used a fixed maximum principal quantum number of 1000, and a maximum orbital angular momentum of 4 for these calculations. For $l > 4$, the analytic hydrogenic radial integrals from the recurrence relations of Burgess (1964) were employed.

2.4. Dielectronic recombination

In photoionized nebulae such as PNe, low-temperature DR is the dominant form of recombination for many species. We therefore computed DR for $\Delta n = 0$ core excitations, neglecting $\Delta n \geq 1$ excitations, which are usually negligible at the temperatures of interest ($\sim 10^4$ K). However, for DR of Se^+ and Se^{2+} (forming Se^0 and Se^+ , respectively), we allowed core excitations into the

$5s$ and $5p$ orbitals since the lowest $4s^2 4p^k 5s$ and $4s^2 4p^k 5p$ ($k = 2, 3$) levels lie below the lowest $4s^2 4p^k 4d$ levels in energy for these ions. Due to the intensive computational requirements of DR calculations, we ignored the (small) contributions to the Se^+ and Se^{2+} DR rate coefficients from excitations into the $5d$, $5f$, and $5g$ orbitals.

In the case of low-temperature DR, it is critical to have accurate energies for low-energy autoionizing states, in order to determine whether they lie just above the ionization threshold and contribute to DR, or just below threshold in which case they do not. Unfortunately, the energies of these levels have not been spectroscopically determined for Se or other n -capture elements, thereby limiting the accuracy of our calculated DR rate coefficients. To alleviate this source of uncertainty, we used experimental target energies whenever possible (Badnell 2006a). When experimental energies are incomplete for a given term, we assumed the theoretical level splitting. We did not attempt to adjust the energies of high-energy terms or configurations that had not been experimentally measured, as done by Badnell (2006a).

We augmented the CI expansions of the structure calculations by including all relevant core excitations for the target ion, allowing for promotions out of the $4s$ and $4p$ subshells. One-electron additions to all target configurations were added to the $(N + 1)$ -electron ion CI expansions to account for final states for the Rydberg electron to radiate into the core.

We determined the DR rate coefficients over the temperature range $(10^1 - 10^7)z^2$ K for each state within the ground configuration. Captures into Rydberg states up to $n = 1000$ and $l = 200$ were computed, with $l \geq 9$ treated hydrogenically for all ions except Se^{5+} , in which $l \geq 11$ states were treated hydrogenically to allow the calculation to converge.

3. Results

3.1. Photoionization cross sections

The photoionization and photoexcitation cross sections from AUTOSTRUCTURE were processed with the ADASPI and ADASPE codes, which respectively produce the *adf39* and *adf38* output files (see Summers 2005, for a detailed description). To simplify the presentation of these results, we used the *xpeppi* post-processing code² to add the direct PI and photoexcitation-autoionization cross sections.

PI cross sections from 0 to 100 Rydbergs for Se^0 – Se^{5+} are presented as supplementary data files available at the CDS, and are illustrated in Fig. 1 for PI out of the ground state of each ion. The photoionization plus photoexcitation-autoionization cross sections (files labeled “seq+XPITOT.dat,” $q = 0 - 5$) are provided for all states in the ground configuration of each ion. In those files, column 1 gives the photon energy relative to the ground state and column 2 the photon energy relative to the initial state. Columns 3 and 4 present the photo-electron energy relative to the ground and initial states, respectively, and in column 5 the cross section is given in Mb. All energies are in Rydbergs. The data for different states are delimited by comment lines (denoted by a # sign in the first column), followed by three numbers indicating the energy of that level relative to the ground state (or the total energy, in the case of the ground state), the total energy of the target state, and the energy order of the initial state (1 for the ground state, 2 for the first excited state, etc.).

We also provide direct PI cross sections without photoexcitation-autoionization resonances, in files labeled

² see <http://amdpp.phys.strath.ac.uk/autos/>

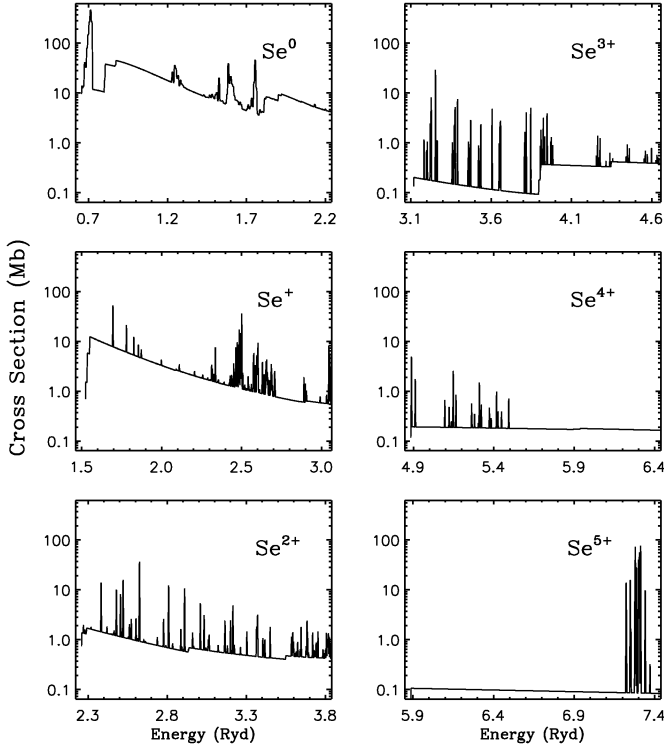


Fig. 1. Ground state PI cross sections for Se^0 – Se^{5+} , in the energy region near the ground state ionization threshold.

“seq+_XDPIOTOT.dat.” In these files, there are two columns, the first of which is the photon energy relative to the ground state, the second the cross section in Mb. Cross sections for different states in the ground configuration are delimited in the same manner as for the seq+_XPITOT.dat files.

3.1.1. Estimation of uncertainties

Special effort was made to estimate uncertainties in the PI cross sections, as these uncertainties affect the accuracy of abundances derived from spectra of astrophysical nebulae (e.g., Sterling et al. 2007). We compared the cross sections computed with the three CI expansions for each ion, and also varied internal parameters or tested assumptions in our calculations (e.g., the values of the scaling parameters for continuum orbitals, the sensitivity to the gauge used, and our orthogonalization of the κ -averaged orbitals). We also compared our results to experimental measurements, as described in the following subsection.

Because we used κ -averaged relativistic wavefunctions, it was necessary to compute the cross sections in the velocity gauge even at the highest energies, where acceleration gauge is optimal. We compared cross sections computed in the length gauge at all energies to those computed solely in velocity gauge. We found negligible differences ($< 1\%$) in the cross sections at both low and high energies, indicating that our use of velocity gauge up to 100 Ryd is not a significant source of error.

For continuum orbitals, we used scaling parameters equal to those of the highest principal quantum number with the same orbital angular momentum for s , p , and d orbitals, and unity for higher angular momentum states. We tested this assumption by calculating PI cross sections with all continuum orbital scaling parameters set to unity. The direct cross sections from these two calculations agree to within 10% (often better) near the

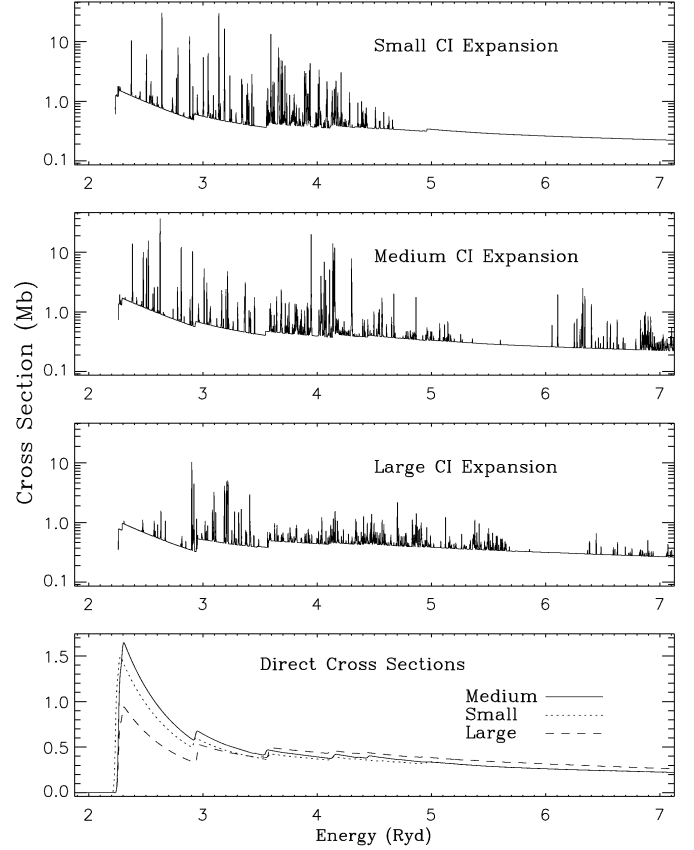


Fig. 2. Comparison of Se^{2+} ground state PI cross sections up to 5 Ryd above the threshold using different CI expansions, as indicated in each of the top three panels. The bottom panel compares the direct PI cross sections, with photoexcitation-autoionization resonances removed, for the three different CI expansions.

ground state threshold for all ions considered, although the resonance strengths vary (especially for Se^+ , where the resonances are weaker by nearly a factor of two when the continuum scaling parameters are 1.0).

For each ion, we also calculated the cross sections without orthogonalizing the radial orbitals. Compared to our calculations with orthogonalized orbitals, the direct PI cross sections agree to within 15% near the ground state threshold of Se^{4+} , and to better than 10% for other ions. However, threshold and resonance energies, as well as resonance strengths, are altered when orthogonalization is not forced, most significantly for the neutral and near-neutral cases. Threshold energies tend to agree best with NIST values for our calculations with orthogonalized radial orbitals, particularly for the neutral and single ion, in which the thresholds are 0.005–0.02 Ryd higher than in the non-orthogonal calculations.

The most significant differences are found from comparing the PI cross sections calculated with different CI expansions. The deviations in the electronic structure for the target and $(N + 1)$ -electron ions lead to disparate resonance energies and strengths, as can be seen in Figs. 2 and 3 for the cases of Se^{2+} and Se^{3+} . The sensitivity of the resonance strengths and positions to the CI expansion and other internal parameters illustrates the challenge of accurately reproducing photoexcitation-autoionization resonances in the distorted-wave approximation.

However, given the uncertainty in PI resonance positions from any type of theoretical calculation, numerical models of

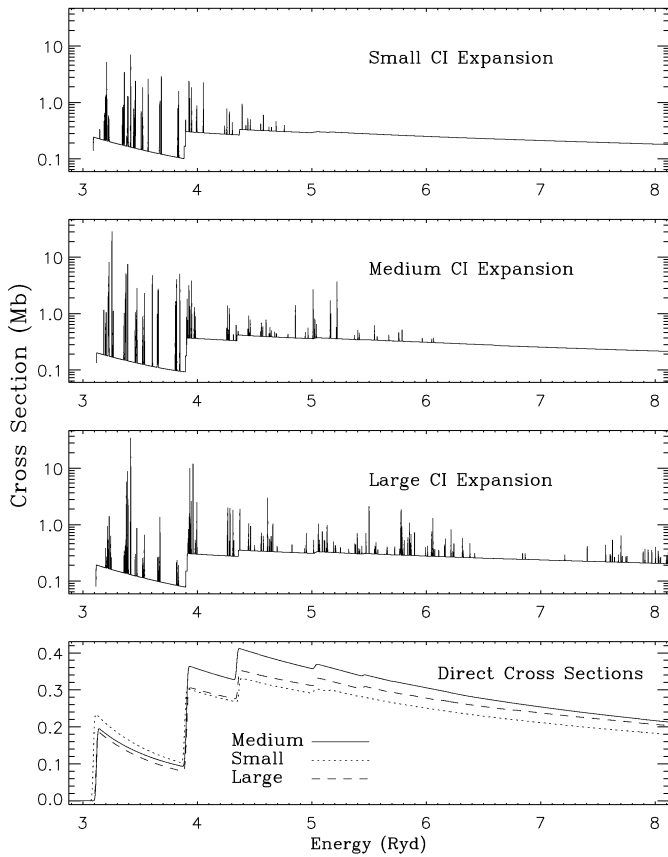


Fig. 3. Comparison of Se^{3+} ground state PI cross sections up to 5 Ryd above the threshold using different CI expansions, as indicated in each of the top three panels. The bottom panel compares the direct PI cross sections, with photoexcitation-autoionization resonances removed, for the three different CI expansions.

ionized astrophysical nebulae often only consider direct PI (e.g., Verner et al. 1996) or convolve the cross section with Gaussians to smooth over the uncertainty in resonance positions (Bautista & Kallman 2001). Indeed, our goal in this work is to best reproduce the direct PI cross sections for low-charge Se ions, and to quantify their uncertainties within the distorted wave approximation.

The bottom panels of Figs. 2 and 3 compare the direct ground state PI cross sections calculated with each of the three CI expansions. In general, the cross sections agree to within roughly 30% for most ions near the ground state ionization threshold. The discrepancy can be as large as 60% in the cases of Se^+ and Se^{2+} , but generally decreases with energy. For Se^{4+} , the direct cross sections agree to within 10% near threshold.

Given these internal tests of our cross sections and our comparisons to experimental measurements (Sec. 3.1.2), we estimate our calculated direct PI cross sections to be uncertain by 30–50% in the energy region near the ground state ionization threshold.

3.1.2. Comparison to experiment

To benchmark and test the accuracy of our results, we have compared our (medium CI expansion) calculations to experimental absolute PI cross-section measurements performed at the ALS synchrotron radiation facility. Se^+ , Se^{2+} , Se^{3+} , and Se^{5+}

cross sections³ were measured from the threshold of the highest-energy metastable state in the ground configuration up to 10 eV beyond the ground state ionization threshold (Esteves et al. 2010). Experimental results for Se^+ (Sterling et al. 2011) and Se^{3+} (Esteves et al. 2009) have been published, and we compare our theoretical results to experiment for those ions in this section (a similar comparison to the as-yet unpublished Se^{2+} and Se^{5+} cross sections was also performed).

The experimental measurements were described by Esteves et al. (2009) and Sterling et al. (2011), and we refer the reader to those papers for full details. Briefly, the PI cross sections were measured via the merged beam method (Lyon et al. 1986). The photoionization spectra were measured by scanning across photon energies, and normalized to an absolute scale with absolute cross-section measurements performed at discrete energies. Overall, uncertainties in the experimental cross sections were estimated to be ~30% for Se^+ and ~20% for Se^{3+} (Sterling et al. 2011; Esteves et al. 2009).

The experimental data are complicated by the fact that the primary ion beams were composed of an unknown admixture of ground and metastable states. We therefore linearly combined the computed cross sections of the ground configuration states to best reproduce the direct experimental cross sections and (when possible) families of resonances.

Figs. 4 and 5 compare our calculated Se^+ and Se^{3+} PI cross sections (solid lines) with experimental measurements (dotted lines). The computed Se^+ cross section was convolved with a Gaussian of 28 meV FWHM to reproduce the experimental resolution. By visual comparison to the experimental data, we found best agreement by weighting the contribution of the ground configuration states ($^4\text{S}_{3/2}$, $^2\text{D}_{3/2}$, $^2\text{D}_{5/2}$, $^2\text{P}_{1/2}$, $^2\text{P}_{3/2}$) by (0.53, 0.15, 0.05, 0.11, 0.16). As expected (see Sect. 3.1.1), our distorted-wave calculations do not accurately reproduce the resonance structure of the experimental PI cross section. In addition, the Fano profile near 1.7 Ryd is not reproduced by our calculations (*R* matrix techniques are necessary to reproduce resonance interference effects), and the lack of this interference causes the discrepancy in the direct cross section in this energy region. The calculated and experimental Se^+ direct cross sections agree to within 30–50% over the range of experimental energies, except above 2.2 Ryd, where the experimental measurements are more uncertain since only a single absolute measurement was made above 1.98 Ryd (compared to absolute measurements at lower energies, where independent estimates were performed 2–3 times for each energy).

The calculated Se^{3+} cross section was convolved with a 20 meV FWHM Gaussian, and we found that statistical weighting of the two ground configuration states provided reasonable agreement with the experimental measurements of Esteves et al. (2009) near threshold. Again, resonance energies and strengths are in poor agreement, though several general resonance families are seen in both the theoretical and experimental results. The computed direct cross section is smaller than that of experiment, but agrees within the noise up to 3.38 Ryd. From 3.38 to 3.9 Ryd, however, an apparent threshold is observed in the experimental data that is not reproduced in our theoretical cross section. In the calculated cross section, the threshold near 3.9 Ryd is due to photoionization into the target $\text{Se}^{4+} 4s 4p^3 \text{P}$ term. The energy of this term is lower than the NIST value, and hence an inaccurate energy for this threshold cannot explain the experimental thresh-

³ The Se^{4+} cross section could not be measured, due to the presence of strong autoionizing states in the parent Se^{4+} ion beam that led to an extremely high background.

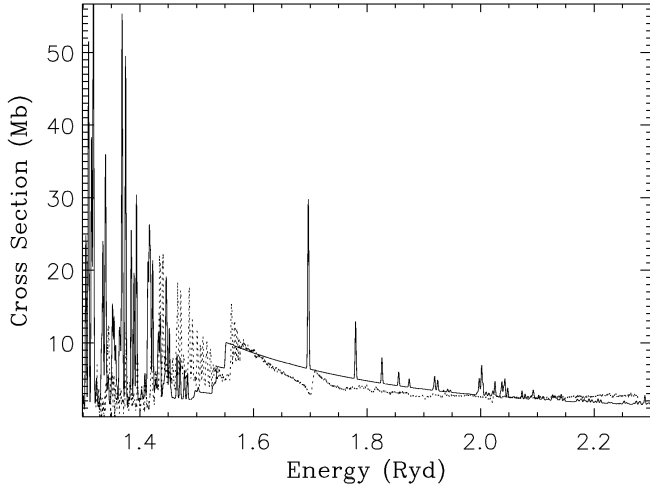


Fig. 4. Comparison of calculated (solid line) and experimental (dotted line) Se^+ PI cross sections. The theoretical curve is a linear combination of the cross sections from the ground configuration ($4S_{3/2}$, $2D_{3/2}$, $2D_{5/2}$, $2P_{1/2}$, $2P_{3/2}$) weighted by the factors (0.53, 0.15, 0.05, 0.11, 0.16), respectively. The theoretical cross section was convolved with a Gaussian of 28 meV FWHM to reproduce the experimental resolution.

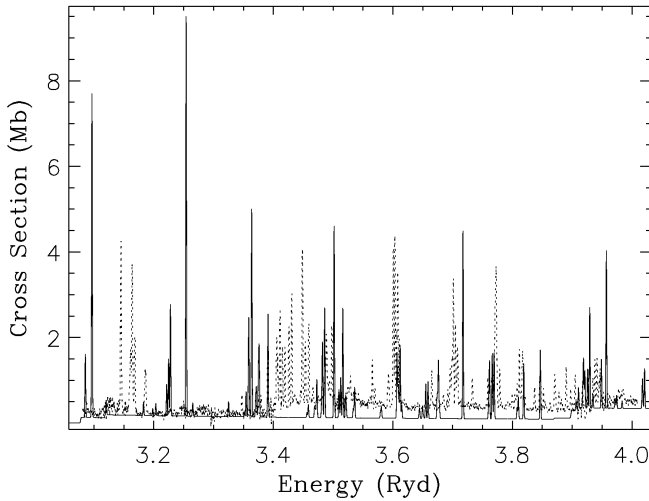


Fig. 5. Comparison of calculated (solid line) and experimental (dotted line) Se^{3+} PI cross sections. The theoretical curve is a statistically-weighted linear combination of the cross sections from the two ground configuration states. The theoretical cross section was convolved with a Gaussian of 20 meV FWHM to reproduce the experimental resolution.

old at 3.38 Ryd. Given that $4s4p^3P$ is the lowest-energy excited term of Se^{4+} and that it is unlikely the primary Se^{3+} ion beam contained metastable states with excitation energies of more than one Rydberg, this experimental feature is puzzling. However, recent revisions to the analysis of the experimental Se^{3+} data indicate that the apparent threshold at 3.38 Ryd is due to a cluster of poorly-resolved resonances, as well as an error in the normalization of the data to an absolute scale at energies above 3.38 Ryd (D. A. Esteves, private communication).

Comparisons to the as-yet unpublished Se^{2+} and Se^{5+} cross sections (not shown in this paper) are more encouraging, at least

in terms of the direct cross sections. In both cases, our calculations agree within the noise of the experimental data.

3.2. Radiative recombination rate coefficients

RR rate coefficients were calculated from the direct photoionization cross sections using the ADASRR code. The resulting *adf48* output files (available at the CDS) are similar in structure to *adf09* files for DR (see Summers 2005, for a detailed description). In these files, partial RR rate coefficients to states with $n \leq 8$ are fully J -resolved, and are bundled over the final outer quantum numbers as bundled- nl for $n \leq 10$, and bundled- n for $n < 1000$ (see Badnell 2006b). At the end of each *adf48* file, total RR rate coefficients are written as a function of temperature for each target ground configuration state.

We fit the rate coefficients with the analytical form (Verner & Ferland 1996; Badnell 2006b)

$$\alpha_{\text{RR}}(T) = A \times \left[\sqrt{T/T_0} (1 + \sqrt{T/T_0})^{1-B_0} (1 + \sqrt{T/T_1})^{1+B_0} \right]^{-1}, \quad (1)$$

where

$$B_0 = B + C \exp(-T_2/T). \quad (2)$$

In this equation, $T_{0,1,2}$ are in temperature units, A and the rate coefficient $\alpha_{\text{RR}}(T)$ have units of $\text{cm}^3 \text{s}^{-1}$, and B and C are dimensionless parameters. For several low-charge states, the RR rate coefficients exhibit large “bumps” at high temperature. These features are caused by electron capture into low principal quantum number states, in which the nucleus is not as effectively screened as for higher states. Equations 1 and 2 are not able to reproduce the size of the bumps, and become inaccurate at high temperatures. For these $\text{Se}^+ - \text{Se}^{3+}$ target states, we therefore fit the high-temperature RR rate coefficients with the function

$$\alpha_{\text{RR}}(T) = \frac{1}{T^{3/2}} \sum_{i=1}^n c_i \exp(-E_i/T), \quad (3)$$

where T and E_i are in temperature units (K), the rate coefficient is in $\text{cm}^3 \text{s}^{-1}$, c_i in $\text{cm}^3 \text{s}^{-1} \text{K}^{3/2}$, and n ranges from 5 to 7 depending on the ion. This analytical function is typically used to fit DR rate coefficients (e.g., Zatsarinny et al. 2003), as done in Sect. 3.3.

The fit coefficients were determined using a non-linear least-squares fit algorithm, generally leading to fit accuracies within 5% for the low-temperature fits, and $\leq 2\%$ at high temperatures. However, the low-temperature fits are only accurate to within 7.5% for Se^+ (level 1) and Se^{3+} (level 1), and the accuracies of the high-temperature fits for Se^+ are 3% (levels 2-4) to 4% (level 5). Moreover, Equations 1 and 2 are unable to reproduce the rate coefficient for RR onto level 5 of Se^+ at the lowest temperatures (≤ 20 K), where they deviate from the calculated rate coefficients by up to 20%. Aside from this exception, the fits have the correct asymptotic forms outside of the temperature range ($10^1 - 10^7$) K (specifically, Equations 1 and 2 describe the asymptotic behavior as $T \rightarrow 0$ K, and Equation 3 correctly describes the rate coefficient at the high-temperature limit).

Table 5 displays the fit coefficients from equations 1 and 2, as well as the maximum temperature T_{max} for which the fits are valid to within the stated accuracies. If T_{max} is not given in Table 5, then equations 1 and 2 are accurate over the full temperature range ($10^1 - 10^7$) K and correctly describe the asymptotic behavior of the rate coefficients at the high-temperature limit. Table 6 provides fit coefficients for the RR rate coefficients from T_{max} to 10^7K . In Fig. 6, we display the ground state RR rate coefficients for low-charge Se ions as a function of temperature.

Table 5. Fit coefficients for radiative recombination rate coefficients at low temperature (see Equations 1 and 2). T_{\max} represents the maximum temperature for which these fits are valid to within the stated accuracies (5%, unless noted). For recombination at temperatures exceeding T_{\max} , the fits from Equation 3 and coefficients listed in Table 6 should be used. If no T_{\max} is given, then the fits are accurate over the entire temperature range ($10^1 - 10^7$) z^2 K. The notation $x(y)$ denotes $x \times 10^y$.

Target Ion ^a	Level	A (cm ³ s ⁻¹)	B	T_0 (K)	T_1 (K)	C	T_2 (K)	T_{\max} (K)
Se ⁺	1 ^b	7.395(-10)	0.7288	7.273(-2)	3.495(6)	0.3306	2.160(6)	...
	2	2.808(-11)	0.4980	3.761	3.415(129)	0.3365	4.621(1)	2.0(3)
	3	2.747(-11)	0.4818	3.926	2.747(111)	0.3515	4.451(1)	2.0(3)
	4 ^c	1.439(-11)	0.0535	2.036(1)	6.815(130)	0.7152	4.065(1)	2.0(3)
	5 ^d	3.719(-11)	0.4765	3.786	3.019(101)	0.2935	6.541(1)	1.0(3)
Se ²⁺	1	6.253(-11)	0.6744	6.081(1)	5.440(5)	0.8633	2.232(6)	8.0(4)
	2	3.804(-12)	0.5422	7.174(3)	3.930(6)	1.3093	1.915(5)	8.0(4)
	3	2.977(-11)	1.0695	3.398(1)	1.907(5)	0.9534	2.179(6)	8.0(4)
	4	1.358(-11)	1.1128	7.719(1)	2.460(5)	1.0094	2.152(6)	8.0(4)
	5	2.109(-11)	1.0811	2.623(1)	2.879(5)	0.8678	2.142(6)	8.0(4)
Se ³⁺	1 ^e	1.496(-11)	0.0000	3.270(3)	9.004(7)	0.7282	1.394(6)	...
	2	5.353(-11)	0.9825	5.028(1)	6.721(5)	1.0127	4.915(5)	9.0(5)
Se ⁴⁺	1	2.664(-11)	0.0000	3.018(3)	1.142(8)	0.6892	1.136(6)	...
Se ⁵⁺	1	5.822(-11)	0.1471	1.562(3)	1.905(8)	0.5119	1.031(6)	...
Se ⁶⁺	1	1.293(-10)	0.3096	8.107(2)	2.554(8)	0.3114	1.278(6)	...

Notes. ^(a) Note that the ion and level numbers correspond to the target ion (i.e., before recombination). ^(b) The fit is accurate to within 7.5%. ^(c) The fit is accurate to within 5% except at the lowest temperature (10 K), where it is accurate to within 7%. ^(d) The fit is accurate to within 5% except at the lowest temperatures (below 20 K), where the fit agreement can be as poor as 20%. For this reason, the fit to the RR rate coefficient for this state should not be considered valid below 20 K. ^(e) The fit is accurate to within 7%.

Table 6. Fit coefficients for radiative recombination rate coefficients at high temperatures, valid from T_{\max} (see Table 5) to $10^7 z^2$ K. See Equation 3. Coefficients c_i are in cm³ s⁻¹ K^{3/2}, and E_i are in K. States whose RR rate coefficients are accurately described by Equations 1 and 2 (with coefficients given in Table 5) over the full temperature range ($10^1 - 10^7$) z^2 K are not listed here. The fits are accurate to within 3% for Se⁺ levels 2–4, 4% for Se⁺ level 5, and $\leq 2\%$ otherwise. The notation $x(y)$ denotes $x \times 10^y$.

Target Ion ^a	Level	c_1	c_2	c_3	c_4	c_5	c_6	c_7
Se ⁺	2	6.380(-8)	3.641(-7)	1.412(-6)	2.856(-6)	6.461(-6)	1.067(-4)	4.751(-4)
	3	6.425(-8)	3.638(-7)	1.403(-6)	2.811(-6)	6.138(-6)	1.018(-4)	4.729(-4)
	4	7.502(-8)	4.203(-7)	1.429(-6)	2.582(-6)	5.538(-6)	8.929(-5)	3.948(-4)
	5	3.371(-8)	1.857(-7)	8.251(-7)	2.939(-6)	5.302(-6)	8.719(-5)	3.936(-4)
	5	3.371(-8)	1.857(-7)	8.251(-7)	2.939(-6)	5.302(-6)	8.719(-5)	3.936(-4)
Se ²⁺	1	2.061(-6)	8.034(-6)	1.447(-5)	2.769(-4)	1.237(-3)	2.609(-3)	...
	2	2.232(-6)	8.551(-6)	1.552(-5)	2.780(-4)	1.240(-3)	2.586(-3)	...
	3	1.018(-5)	1.613(-5)	2.749(-4)	1.236(-3)	2.612(-3)
	4	1.195(-5)	7.588(-5)	6.316(-4)	1.965(-3)	4.432(-3)
	5	5.306(-6)	7.409(-6)	7.781(-5)	5.502(-4)	1.469(-3)	2.035(-3)	...
Se ³⁺	2	4.289(-5)	1.638(-3)	1.161(-2)	5.245(-3)	2.772(-2)
		E_1	E_2	E_3	E_4	E_5	E_6	E_7
Se ⁺	2	6.920(2)	6.054(3)	2.936(4)	1.100(5)	6.510(5)	3.218(6)	1.207(7)
	3	6.990(2)	6.080(3)	2.926(4)	1.087(5)	6.306(5)	3.137(6)	1.190(7)
	4	6.984(2)	6.165(3)	2.893(4)	1.029(5)	6.244(5)	3.151(6)	1.194(7)
	5	3.045(2)	2.838(3)	1.405(4)	6.763(4)	5.084(5)	3.075(6)	1.182(7)
	5	3.045(2)	2.838(3)	1.405(4)	6.763(4)	5.084(5)	3.075(6)	1.182(7)
Se ²⁺	1	3.108(3)	4.135(4)	3.780(5)	2.581(6)	1.008(7)	3.998(7)	...
	2	4.231(3)	4.997(4)	4.748(5)	2.637(6)	1.015(7)	4.037(7)	...
	3	3.628(4)	4.849(5)	2.644(6)	1.019(7)	4.124(7)
	4	6.274(4)	1.334(6)	5.185(6)	2.057(7)	1.135(8)
	5	2.145(4)	1.718(5)	1.457(6)	5.086(6)	1.786(7)	6.142(7)	...
Se ³⁺	2	6.867(4)	1.119(6)	3.421(6)	2.101(7)	9.183(7)

Notes. ^(a) Note that the ion and level numbers correspond to the target ion (i.e., before recombination).

3.2.1. Estimation of uncertainties

We tested the sensitivity of the calculated RR rate coefficients to the use of different CI expansions and other internal parameters in our calculations. The uncertainties that we discuss were estimated at temperatures near 10^4 K, similar to electron temperatures in photoionized nebulae.

As is the case for PI, the RR rate coefficients are most sensitive to the CI expansion used. The rate coefficients calculated with the small and large configuration sets (Table 1) differ from the presented rate coefficients (from the medium CI expansion) typically by less than 10% near 10^4 K. The sole exception is that of Se⁺, for which the deviation from the presented rate coefficients is 25–30%.

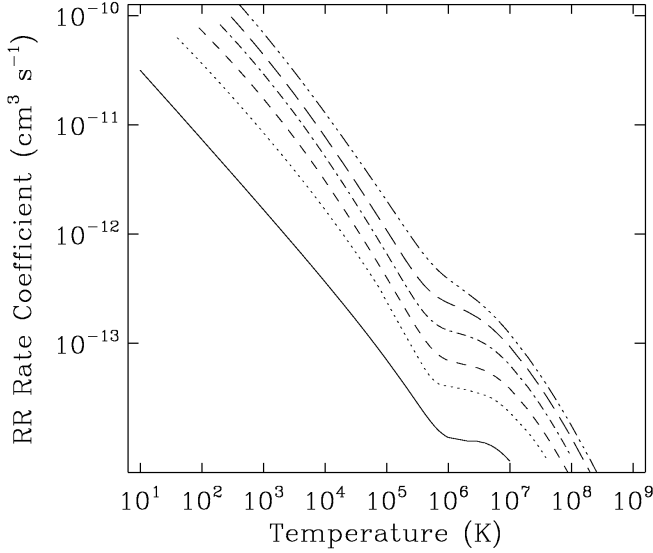


Fig. 6. Radiative recombination rate coefficients as a function of temperature for ground state target ions Se^+ (solid curve), Se^{2+} (dotted curve), Se^{3+} (short-dashed curve), Se^{4+} (dash-dot-dash curve), Se^{5+} (long-dashed curve), and Se^{6+} (dash-dot-dot-dash curve).

Other tested parameters produced smaller changes in the RR rate coefficients. For example, to test the sensitivity of forcing velocity gauge at high energies, we computed the rate coefficients from PI cross sections cut off at the maximum velocity gauge energy (beyond which velocity gauge must be forced in AUTOSTRUCTURE). The RR rate coefficients were unaffected except at the highest temperatures (typically a few times 10^5 – 10^6 K). This indicates that uncertainties associated to our use of velocity gauge at high energies are negligible for the computed RR rate coefficients at photoionized plasma temperatures, and become important only above 10^5 K for singly- and doubly-charged Se, and above 10^6 K for higher charge states.

The calculations were performed using 3 interpolation energies per decade. We tested the effects of using a finer interpolation mesh of five energies per decade, and found differences of less than 1% in the RR rate coefficients for all of the investigated Se ions. Similarly, the use of target ion scaling parameters versus those of the $N + 1$ -electron ion produced discrepancies in the rate coefficients larger than 1% only in the case of Se^+ and Se^{2+} , where the differences are 3–7% (depending on the state) near 10^4 K. Finally, we computed RR rate coefficients without Schmidt orthogonalizing the radial orbitals, and found that the rate coefficient differed by a maximum of 1–3% (for Se^+ and Se^{2+}) compared to our orthogonalized calculations.

We conclude that our computed RR rate coefficients have internal uncertainties of less than 10% with the exception of Se^+ , where the uncertainty is 30–40%.

3.3. Dielectronic recombination rate coefficients

DR rate coefficients were computed from the resonant photoionization cross sections with the ADASDR code, and the *adf09* output files are available at the CDS (see Summers 2005, for a detailed description of the structure of these files). The rate coefficients were fitted with functions of the form Equation 3, with n ranging between 5 and 7 (see Table 7). The fits for most ions are accurate to within 5% over the temperature range $(10^1 - 10^7)z^2$ K,

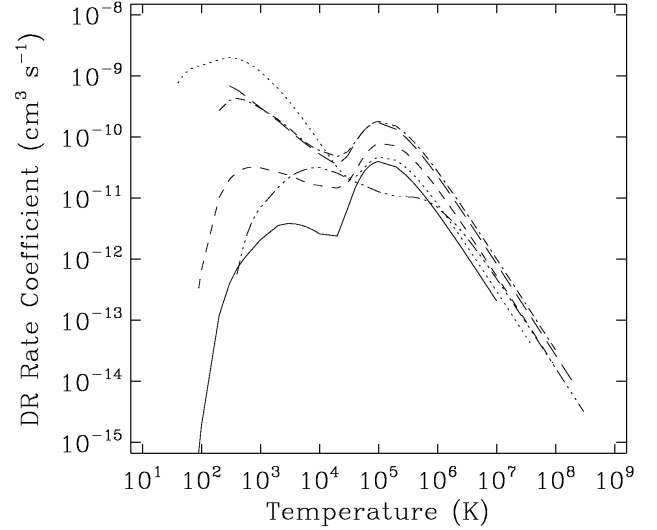


Fig. 7. Dielectronic recombination rate coefficients as a function of temperature for ground state target ions Se^+ (solid curve), Se^{2+} (dotted curve), Se^{3+} (short-dashed curve), Se^{4+} (dash-dot-dash curve), Se^{5+} (long-dashed curve), and Se^{6+} (dash-dot-dot-dash curve).

and reproduce the correct asymptotic behavior outside of this temperature range. The fitting algorithm was not able to accurately reproduce the rate coefficient behavior over the full temperature range for DR onto level 4 (the third excited state) of the Se^{2+} target. That fit is not valid below 80 K, and is only accurate to within 11% near 2000 and 40000 K (but to better than 2% at other temperatures). DR onto level 2 of Se^+ is also fit less accurately, to within 6%.

Fig. 7 illustrates the DR rate coefficients over the temperature range $(10^1 - 10^7)z^2$ K. This figure reveals that while the rate coefficients exhibit similar behavior at high temperatures ($> 10^6$ K), there are marked differences in their magnitudes and behavior at lower temperatures due to the differing resonance structure near their ionization thresholds.

Fig. 8 compares the RR, DR, and total recombination rate coefficients for each of the first six Se ions. From this plot, it is apparent that DR dominates RR for each ion at 10^4 K, with rate coefficients larger by as much as two orders of magnitude (and occasionally even more at other temperatures). The RR rate coefficient becomes comparable to that of DR at temperatures higher than 10^7 K for some ions, though this is likely due to the fact that we did not consider DR from $\Delta n > 0$ core excitations, which become important at high temperatures. RR dominates DR only at low temperatures (less than 1000–5000 K) for Se^+ , Se^{3+} , and Se^{6+} . This highlights the importance of obtaining accurate DR rate coefficients, as it is the principal recombination process for low-charge Se ions (and indeed for many other heavy elements, as noted for example by Badnell 2006a; Altun et al. 2007; Nikolić et al. 2010) in photoionized nebulae.

3.3.1. Estimation of uncertainties

At photoionized plasma temperatures, DR proceeds via electron capture into low-lying autoionizing states. Unfortunately, the energies of these states have not been determined for the vast majority of atomic ions beyond the second row of the Periodic Table. Inaccuracies in the calculated energies of

Table 7. Fit coefficients for dielectronic recombination rate coefficients; see Equation 3. Coefficients c_i are in $\text{cm}^3 \text{s}^{-1} \text{K}^{3/2}$, and E_i are in K. The fits are accurate to within 5% over the temperature range $(10^1 - 10^7)z^2$ K, unless otherwise noted. The notation $x(y)$ denotes $x \times 10^y$.

Target Ion ^a	Level	c_1	c_2	c_3	c_4	c_5	c_6	c_7
Se ⁺	1	5.895(-8)	1.516(-7)	2.154(-6)	4.509(-6)	7.933(-4)	2.944(-3)	2.944(-3)
	2 ^b	4.849(-9)	4.750(-8)	1.915(-7)	1.839(-6)	1.633(-4)	2.211(-3)	7.745(-6)
	3	2.580(-8)	4.667(-8)	2.042(-6)	2.148(-3)	5.616(-4)
	4	2.086(-8)	2.435(-7)	2.120(-6)	3.332(-7)	3.652(-6)	1.713(-3)	1.929(-4)
	5	2.547(-7)	1.297(-7)	4.131(-4)	2.075(-3)	2.433(-6)
Se ²⁺	1	4.841(-6)	4.993(-5)	3.566(-5)	9.558(-5)	9.458(-3)	1.988(-5)	...
	2	1.830(-6)	5.312(-6)	1.432(-5)	2.280(-5)	5.604(-3)	2.176(-3)	...
	3	1.686(-8)	2.146(-7)	5.827(-7)	2.436(-6)	1.391(-4)	6.526(-3)	...
	4 ^c	3.875(-8)	1.641(-6)	3.522(-3)	3.732(-3)	-3.333(-4)
	5	7.246(-13)	9.784(-9)	3.270(-6)	2.470(-5)	2.923(-4)	1.598(-3)	1.609(-3)
Se ³⁺	1	1.268(-6)	2.651(-6)	1.386(-5)	1.166(-4)	3.731(-3)	6.768(-3)	6.499(-3)
	2	2.286(-6)	3.420(-6)	4.948(-5)	4.206(-4)	1.030(-2)
Se ⁴⁺	1	1.505(-5)	3.440(-5)	2.571(-4)	2.806(-3)	2.952(-2)
Se ⁵⁺	1	1.107(-5)	2.896(-5)	8.937(-5)	6.877(-5)	1.457(-2)	1.213(-2)	...
Se ⁶⁺	1	2.771(-6)	3.733(-5)	1.459(-4)	7.999(-4)	5.106(-3)	1.052(-2)	...
		E_1	E_2	E_3	E_4	E_5	E_6	E_7
Se ⁺	1	1.036(3)	1.963(3)	4.529(3)	1.464(4)	1.217(5)	1.754(5)	1.772(5)
	2 ^b	8.714(1)	2.241(2)	7.538(2)	1.046(4)	9.325(4)	1.525(5)	1.764(6)
	3	9.716(1)	1.663(3)	1.077(4)	1.330(5)	2.180(5)
	4	2.655(2)	3.997(2)	9.086(2)	1.797(3)	3.584(4)	1.336(5)	2.199(5)
	5	8.821(2)	2.098(3)	9.386(4)	1.423(5)	8.491(5)
Se ²⁺	1	1.289(2)	5.862(2)	1.935(3)	7.117(4)	1.957(5)	1.719(6)	...
	2	6.188(1)	3.923(2)	2.220(3)	3.978(4)	1.797(5)	2.263(5)	...
	3	4.308(2)	9.211(2)	3.360(3)	1.096(4)	8.181(4)	1.899(5)	...
	4 ^c	4.521(3)	1.678(4)	1.429(5)	2.330(5)	5.738(5)
	5	1.158(3)	5.031(3)	1.522(4)	3.687(4)	9.171(4)	1.416(5)	1.657(5)
Se ³⁺	1	7.565(2)	1.959(3)	6.654(3)	3.054(4)	1.518(5)	2.134(5)	2.156(5)
	2	6.470(2)	3.122(3)	1.519(4)	6.767(4)	1.908(5)
Se ⁴⁺	1	5.954(2)	3.483(3)	2.477(4)	1.053(5)	1.886(5)
Se ⁵⁺	1	3.417(2)	2.862(3)	1.556(4)	4.233(4)	1.420(5)	1.941(5)	...
Se ⁶⁺	1	2.567(3)	8.368(3)	2.392(4)	1.260(5)	5.466(5)	1.186(6)	...

Notes. ^(a) Note that the ion and level numbers correspond to the target ion (i.e., before recombination). ^(b) The fit is accurate to within 6%. ^(c) The rate coefficient for DR onto level 4 of the Se²⁺ target could not be fit to accuracies as high as other levels and ions, and is not valid below 80 K. The fit is only accurate to within 11% near 2 000 and 40 000 K, but to within 2% at all other temperatures.

these near-threshold autoionizing resonances are thus the chief source of uncertainty in computed low-temperature DR rate coefficients (see, e.g., Savin et al. 1999; Ferland 2003). While Robicheaux et al. (2010) showed that thermal broadening of the continuum threshold in finite density plasmas alleviates to some extent the problem of identifying which resonances lie just above the threshold (and can contribute to DR) and which do not, this effect is not likely to be sufficiently large to mitigate the comparatively large uncertainties in resonance positions resulting from theoretical calculations.

To estimate the uncertainties in our calculated DR rate coefficients due to the unknown energies of near-threshold autoionizing resonances, we shifted the continuum threshold by the amount of the largest discrepancy in calculated versus experimental target energies, with the direction of the shift determined by whether the computed energies were too large or too small relative to experiment. For DR onto the ground state of target ions, this resulted in discrepancies in the rate coefficient near 10^4 K of 15–30% for Se³⁺ and Se⁴⁺, a factor of two for Se⁵⁺, a factor of 4–5 for Se⁶⁺, and 1–2 orders of magnitude for Se²⁺ and Se⁺ (respectively).

We also compared the DR rate coefficients computed with the small and medium configuration sets (due to the computationally intensive nature of the DR calculations, we did not

attempt to compute rate coefficients for the large configuration sets). These uncertainties were much smaller than obtained from shifting the continuum threshold, leading to differences of 5–30% near 10^4 K with the exception of the Se⁺ target (factor of 4 difference).

Clearly, the uncertainties in the DR rate coefficients are much larger than those for PI or RR. Because DR dominates RR at photoionized plasma temperatures for these Se ions (and indeed many other heavy atomic ions), this remains an important problem for modeling photoionized astrophysical nebulae. Since the energies of near-threshold autoionizing resonances have not been experimentally determined and are extremely difficult to accurately calculate even with the most sophisticated theoretical methods, the solution to this important problem will be challenging to achieve.

Perhaps the most reliable method of obtaining highly accurate DR rate coefficients is electron-ion beam merging techniques with heavy-ion storage rings such as the TSR (Savin et al. 1999, 2006; Schippers et al. 2011). Unfortunately, it is extremely challenging to use storage ring experiments to measure DR rate coefficients of low charge-to-mass species such as the Se ions investigated in this paper. The lowest charge-to-mass ion whose recombination rate coefficient has been experimentally determined is Se³⁺, with $q/m = 1/15$ (Schippers et al. 2002).

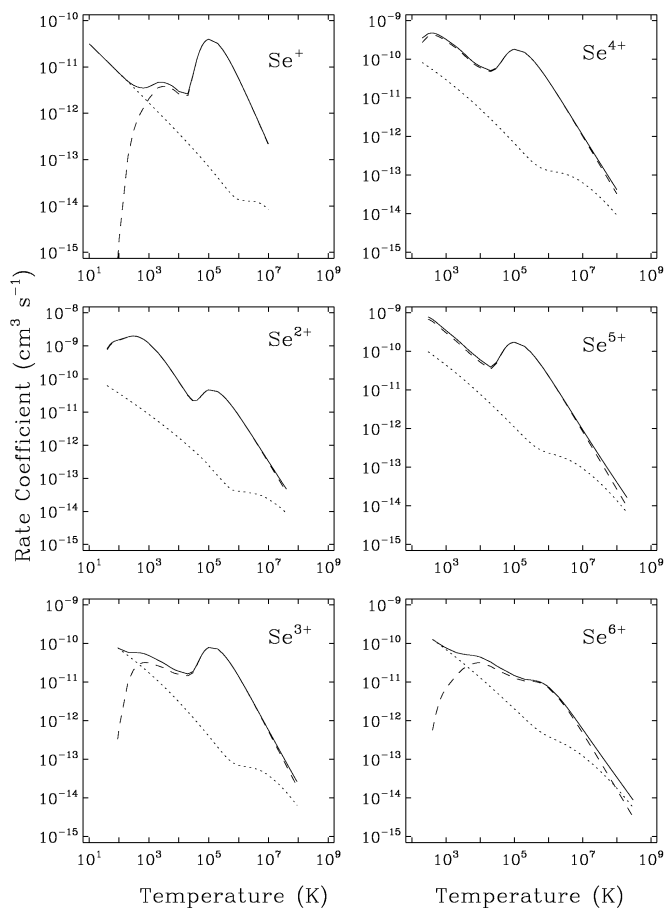


Fig. 8. Comparison of the radiative (dotted curves), dielectronic (dashed curves), and total recombination rate coefficients (solid curves) for each of the first six Se ions.

The maximum bending power of the dipole magnets on current storage ring facilities is the limiting factor for low q/m species, which cannot be stored at sufficiently high energies. If the ion energy is too low, then electron capture during collisions with residual gas molecules produces a very high background that prevents rate coefficient measurements (S. Schippers, private communication; Schippers et al. 2002). Thus, experimental DR measurements of low-charge Se ions are extremely difficult if not impossible with existing storage ring facilities. However, the forthcoming Cryogenic Storage Ring (CSR) facility in Heidelberg will use electrostatic deflectors in place of bending magnets to store the ions, and the residual gas pressure will be much smaller than in the TSR (Wolf et al. 2006). The CSR will enable low-temperature DR rate coefficients to be measured for many low q/m species, including those of trans-iron elements.

4. Concluding remarks

We have presented MCBP calculations of the electronic structure, distorted-wave PI cross sections (including both direct and resonant contributions), and RR and DR rate coefficients for the first six ions of the trans-iron element Se. All of the PI, RR, and DR data are available at the CDS, and analytical fits to the RR and DR rate coefficients are presented in Tables 5, 6, and 7.

These atomic data are critical for efforts to determine the abundance of Se in photoionized astrophysical nebulae.

Se has been detected in dozens of planetary nebulae (Sterling & Dinerstein 2008) and other astrophysical nebulae (see Sect. 1), and is a potentially important tracer of n -capture nucleosynthesis and the chemical evolution of trans-iron elements.

In our calculations, we tested the sensitivity of our results to the use of different configuration expansions and to other internal parameters of the AUTOSTRUCTURE code, in order to provide estimates of the (internal) uncertainties of the presented atomic data. In the case of PI, we also compared our cross sections to recent experimental measurements (Esteves et al. 2009, 2010; Sterling et al. 2011) to gauge the accuracy of our results. We find that the direct PI cross sections for these Se ions are uncertain by 30–50%, while the RR rate coefficients are uncertain by <10% except for Se^+ (~30–40%). Our DR rate coefficients exhibit larger uncertainties (from 15–30% up to 1–2 orders of magnitude) due to the unknown energies of low-lying autoionizing states. The importance of uncertainties in DR rate coefficients is highlighted by the dominance of DR over RR near 10^4 K, the typical temperature of photoionized nebulae such as PNe.

These uncertainties are significant, particularly for the near-neutral cases. Low-charge Se ions are complex systems for which no comprehensive photoionization or recombination data existed prior to our study. Thus one of our goals in addition to producing these data was to provide realistic internal uncertainties, whose effect on nebular abundance determinations can be quantified through numerical simulations of ionized nebulae. Such an investigation will help to target the ionic systems and atomic processes that require further analysis.

This paper is the first in a series to present atomic data for the photoionization and recombination properties of trans-iron elements. In future papers, we will present similar data for Kr and Xe, as well as charge exchange rate coefficients for low-charge ions of several n -capture elements. The ultimate goal of this study is to produce atomic data for n -capture elements that are suitable to be incorporated into photoionization codes that numerically simulate the ionization and thermal structure of astrophysical nebulae. Photoionization codes can be used to derive analytical ionization corrections needed to accurately estimate the abundances of unobserved Se, Kr, and Xe ions in ionized nebulae – and hence to determine their elemental abundances. Our efforts will thus enable much more accurate and robust abundance determinations of trans-iron elements in astrophysical nebulae than was previously possible.

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Table 1. Configuration-interaction expansions used for each Se ion.

Ion	Config. Set ^a	Configurations
Se ⁰	Small (10)	4s ² 4p ⁴ , 4s 4p ⁵ , 4p ⁶
	Medium (326)	4s ² 4p ⁴ , 4s ² 4p ³ 4d, 4s ² 4p ³ 4f, 4s ² 4p ³ 5s, 4s ² 4p ³ 5p, 4s ² 4p ² 4d 5p, 4s 4p ⁵ , 4s 4p ⁴ 5p, 4s 4p ³ 5p ² , 4p ⁶
	Large (785)	4s ² 4p ⁴ , 4s ² 4p ³ 4d, 4s ² 4p ³ 4f, 4s ² 4p ³ 5s, 4s ² 4p ³ 5p, 4s ² 4p ³ 5d, 4s ² 4p ² 4d ² , 4s ² 4p ² 4d 5p, 4s 4p ⁵ , 4s 4p ⁴ 4d, 4s 4p ⁴ 5s, 4s 4p ⁴ 5p, 4s 4p ³ 4d 5s, 4s 4p ³ 5p ² , 4p ⁶ , 3d ⁹ 4s ² 4p ⁵
Se ⁺	Small (15)	4s ² 4p ³ , 4s 4p ⁴ , 4p ⁵
	Medium (189)	4s ² 4p ³ , 4s ² 4p ² 4d, 4s ² 4p ² 5s, 4s ² 4p ² 5p, 4s ² 4p 4d ² , 4s 4p ⁴ , 4s 4p ³ 4d, 4p ⁵
	Large (886)	4s ² 4p ³ , 4s ² 4p ² 4d, 4s ² 4p ² 5s, 4s ² 4p ² 5p, 4s ² 4p ² 5d, 4s ² 4p 4d ² , 4s ² 4p 4d 5s, 4s ² 4p 4d 5d, 4s 4p ⁴ , 4s 4p ³ 4d, 4s 4p ² 4d ² , 4p ⁵ , 4p ⁴ 4d, 4p ⁴ 5s
Se ²⁺	Small (32)	4s ² 4p ² , 4s ² 4p 4d, 4s 4p ³ , 4p ⁴
	Medium (135)	4s ² 4p ² , 4s ² 4p 4d, 4s 4p ³ , 4s 4p ² 4d, 4p ⁴ , 4p ² 4d ² , 3d ⁹ 4s ² 4p ³
	Large (765)	4s ² 4p ² , 4s ² 4p 4d, 4s ² 4p 5s, 4s ² 4p 5p, 4s ² 4p 5d, 4s ² 4d ² , 4s ² 4d 5d, 4s 4p ³ , 4s 4p ² 4d, 4s 4p ² 4f, 4s 4p 4d ² , 4p ⁴ , 4p ³ 4d, 4p ³ 5s, 3d ⁹ 4s ² 4p ² 4d, 3d ⁹ 4s ² 4p 4d 5s
Se ³⁺	Small (40)	4s ² 4p, 4s ² 4d, 4s 4p ² , 4s 4p 4d, 4p ³
	Medium (252)	4s ² 4p, 4s ² 4d, 4s 4p ² , 4s 4p 4d, 4s 4d ² , 4p ³ , 4p ² 4d, 3d ⁹ 4s ² 4p 4d, 3d ⁹ 4s 4p ³
	Large (546)	4s ² 4p, 4s ² 4d, 4s ² 5s, 4s 4p ² , 4s 4p 4d, 4s 4p 4f, 4s 4p 5s, 4s 4p 5p, 4s 4p 5d, 4s 4d ² , 4s 4d 5s, 4s 4d 5p, 4p ³ , 4p ² 4d, 4p ² 5p, 4p 4d ² , 4p 4d 5s, 3d ⁹ 4s ² 4p 4d, 3d ⁹ 4s ² 4d ² , 3d ⁹ 4s ² 4d 5s, 3d ⁹ 4s 4p ³
Se ⁴⁺	Small (10)	4s ² , 4s 4p, 4p ²
	Medium (47)	4s ² , 4s 4p, 4s 4d, 4s 5s, 4p ² , 4p 4d, 4d 5d, 5s ²
	Large (891)	4s ² , 4s 4p, 4s 4d, 4s 5s, 4s 5p, 4s 5d, 4p ² , 4p 4d, 4p 5s, 4p 5p, 4d ² , 4d 5s, 4d 5d, 5s ² , 5p ² , 3d ⁹ 4s ² 4d, 3d ⁹ 4s ² 5d, 3d ⁹ 4s 4p ² , 3d ⁹ 4s 4p 4d, 3d ⁹ 4s 4p 4f, 3d ⁹ 4s 4f 5p, 3d ⁹ 4s 5s 5d
Se ⁵⁺	Small (3)	4s, 4p
	Medium (5)	4s, 4p, 4d
	Large (745)	4s, 4p, 4d, 5s, 5p, 3d ⁹ 4s 4d, 3d ⁹ 4s 5d, 3d ⁹ 4p 4d, 3d ⁹ 4p 4f, 3d ⁹ 4p 5d, 3d ⁹ 4d ² , 3d ⁹ 4d 5s, 3d ⁹ 4d 5p, 3d ⁹ 4d 5d, 3d ⁹ 5s 5p
Se ⁶⁺	Small (35) ^b	3d ¹⁰ , 3d ⁹ 4s, 3d ⁹ 4p, 3d ⁹ 4d
	Medium (35) ^b	3d ¹⁰ , 3d ⁹ 4s, 3d ⁹ 4p, 3d ⁹ 4d
	Large (57)	3d ¹⁰ , 3d ⁹ 4s, 3d ⁹ 4p, 3d ⁹ 4d, 3d ⁹ 5s, 3d ⁹ 5d

Notes. ^(a) After the name of each configuration set, the number of levels is listed in parentheses. ^(b) Although the same CI expansion was utilized for the small and medium sets of Se⁶⁺, the scaling parameters of the medium set were optimized differently: the configurations 3d⁹ 5d, 3d⁹ 6d, and 3d⁹ 7d were included in the configuration list to determine scaling parameters, but removed in the final structure calculation.

Table 2. Radial scaling parameters used for CI expansions of each ion

Se ⁰			
Orbital	Small	Medium	Large
1s	1.25936	1.25385	1.25535
2s	1.09800	1.09813	1.09987
2p	1.06516	1.06543	1.06445
3s	1.02964	1.02983	1.03142
3p	1.01691	1.01707	1.01706
3d	0.98901	0.98953	0.98912
4s	0.96050	0.96355	0.96485
4p	0.97914	0.98363	0.98332
4d	...	1.00469	1.03918
4f	...	1.02392	1.01451
5s	...	0.97193	1.03068
5p	...	1.03442	1.02918
5d	1.01438
Se ⁺			
Orbital	Small	Medium	Large
1s	1.25216	1.25516	1.25364
2s	1.09851	1.09631	1.09585
2p	1.06482	1.06447	1.06307
3s	1.03101	1.02970	1.03059
3p	1.01607	1.01610	1.01536
3d	0.98874	0.98929	0.98970
4s	0.96953	0.96867	0.97226
4p	0.97901	0.98050	0.97058
4d	...	0.99909	0.99017
5s	...	0.98123	0.98732
5p	...	1.01508	1.02418
5d	1.03819
Se ²⁺			
Orbital	Small	Medium	Large
1s	1.26607	1.25544	1.25389
2s	1.09894	1.09742	1.09713
2p	1.06384	1.06381	1.06429
3s	1.03177	1.03118	1.03111
3p	1.01549	1.01509	1.01696
3d	0.98797	0.98820	0.98923
4s	0.97518	0.98274	0.97642
4p	0.98166	0.98982	0.99900
4d	0.98458	0.98379	1.00493
4f	1.09951
5s	0.98270
5p	1.01451
5d	1.02193
Se ³⁺			
Orbital	Small	Medium	Large
1s	1.25706	1.25957	1.25060
2s	1.09599	1.09701	1.09890
2p	1.06234	1.06303	1.06278
3s	1.02897	1.03152	1.03118
3p	1.01422	1.01569	1.01614
3d	0.98716	0.98855	0.98899
4s	0.97684	0.97863	0.98035
4p	0.98730	1.00378	1.00134
4d	0.97966	1.00165	1.00353
4f	1.04938
5s	1.01012
5p	0.97718
5d	0.97798
Se ⁴⁺			
Orbital	Small	Medium	Large
1s	1.25396	1.26031	1.26001
2s	1.09493	1.09398	1.09585
2p	1.06204	1.06105	1.06283
3s	1.02798	1.02729	1.02992
3p	1.01276	1.01272	1.01453
3d	0.98639	0.98662	0.98858
4s	0.97686	0.97774	0.98177
4p	0.97413	0.98345	0.97896
4d	...	0.96499	0.99410
4f	1.03288
5s	...	1.00779	1.02644
5p	0.96971
5d	0.99887

Table 2. Continued.

Se ⁵⁺			
Orbital	Small	Medium	Large
1s	1.26114	1.25370	1.25921
2s	1.09560	1.09502	1.09944
2p	1.06089	1.05993	1.06193
3s	1.02749	1.02797	1.03420
3p	1.01136	1.01121	1.01392
3d	0.98493	0.98512	0.98800
4s	0.97805	0.97821	0.98381
4p	0.97409	0.97389	1.00989
4d	...	0.96765	1.00662
4f	1.01505
5s	1.01864
5p	1.01194
5d	0.99808
Se ⁶⁺			
Orbital	Small	Medium	Large
1s	1.25708	1.25307	1.25533
2s	1.09531	1.09680	1.09484
2p	1.05923	1.05934	1.05967
3s	1.02647	1.02599	1.02605
3p	1.00974	1.00941	1.00948
3d	0.98305	0.98296	0.98285
4s	1.00424	1.00419	1.00427
4p	0.99619	0.99617	0.99622
4d	0.97412	0.97553	0.97555
5s	0.99360
5d	0.97139

Table 3. Comparison of selected calculated and experimental energies (in Rydbergs)

Se ⁰						
Index	Config.	Term	Small	Medium	Large	NIST
1	4s ² 4p ⁴	³ P ₂	0.0000	0.0000	0.0000	0.0000
2		³ P ₁	0.0172	0.0177	0.0177	0.0181
3		³ P ₀	0.0223	0.0225	0.0227	0.0231
4		¹ D ₂	0.1085	0.1034	0.1053	0.0873
5		¹ S ₀	0.1960	0.1826	0.1929	0.2045
6	4s ² 4p ³ 5s	⁵ S ₂	...	0.3945	0.4302	0.4391
7		³ S ₁	...	0.4307	0.4791	0.4647
8	4s ² 4p ³ 5p	⁵ P ₁	...	0.4964	0.5225	0.5399
9		⁵ P ₂	...	0.4974	0.5233	0.5403
10		⁵ P ₃	...	0.4991	0.5249	0.5412
11	4s ² 4p ³ 4d	⁵ D ₂	...	0.5347	0.5533	0.5776
12		⁵ D ₁	...	0.5347	0.5533	0.5775
13		⁵ D ₃	...	0.5347	0.5533	0.5776
14		⁵ D ₀	...	0.5347	0.5532	0.5776
15		⁵ D ₄	...	0.5348	0.5534	0.5776
16	4s ² 4p ³ 5p	³ P ₁	...	0.5396	0.5636	0.5524
17		³ P ₂	...	0.5404	0.5645	0.5529
18		³ P ₀	...	0.5409	0.5649	0.5804
19	4s ² 4p ³ 4d	³ D ₁	...	0.5452	0.5760	0.5951
20		³ D ₂	...	0.5462	0.5764	0.5949
21		³ D ₃	...	0.5478	0.5776	0.5954
22	4s ² 4p ³ 5s	³ D ₂	...	0.5569	0.5907	0.5634
23		³ D ₁	...	0.5571	0.5902	0.5621
24		³ D ₃	...	0.5584	0.5925	0.5672
25		¹ D ₂	...	0.5701	0.6134	0.5785
I.P.	0.6377	0.6558	0.6590	0.7168
Se ⁺						
Index	Config.	Term	Small	Medium	Large	NIST
1	4s ² 4p ³	⁴ S _{3/2}	0.0000	0.0000	0.0000	0.0000
2		² D _{3/2}	0.1527	0.1470	0.1413	0.1200
3		² D _{5/2}	0.1581	0.1520	0.1457	0.1256
4		² P _{1/2}	0.2204	0.2218	0.2104	0.2099
5		² P _{3/2}	0.2267	0.2277	0.2156	0.2177
6	4s 4p ⁴	⁴ P _{5/2}	0.7851	0.7569	0.7460	0.7643
7		⁴ P _{3/2}	0.8001	0.7708	0.7582	0.7799
8		⁴ P _{1/2}	0.8081	0.7783	0.7647	0.7877
9	4s ² 4p ² 5s	⁴ P _{1/2}	...	0.9045	0.8912	0.8682
10		⁴ P _{3/2}	...	0.9145	0.9002	0.8817
11		⁴ P _{5/2}	...	0.9289	0.9129	0.8992
12		² P _{1/2}	...	0.9433	0.9254	0.9012
13		² P _{3/2}	...	0.9523	0.9276	0.9236
14	4s ² 4p ² 5p	² D _{5/2}	...	1.0396	1.0192	0.9874
15		² D _{3/2}	...	1.0399	1.0187	0.9883
16		² S _{1/2}	...	1.0541	1.0644	1.0699
I.P.	1.5128	1.5242	1.5388	1.5574
Se ²⁺						
Index	Config.	Term	Small	Medium	Large	NIST
1	4s ² 4p ²	³ P ₀	0.0000	0.0000	0.0000	0.0000
2		³ P ₁	0.0135	0.0142	0.0158	0.0000
3		³ P ₂	0.0315	0.0334	0.0362	0.0000
4		¹ D ₂	0.1383	0.1406	0.1407	0.1188
5		¹ S ₀	0.2424	0.2710	0.2595	0.2591
6	4s 4p ³	³ D ₁	0.7935	0.8376	0.8308	0.8301
7		³ D ₂	0.7937	0.8378	0.8313	0.8450
8		³ D ₃	0.7967	0.8412	0.8353	0.8798
9		³ P ₂	0.9267	0.9727	0.9654	0.9706
10		³ P ₀	0.9274	0.9735	0.9675	0.9703
11	4s ² 4p 4d	³ P ₁	0.9275	0.9737	0.9676	0.9713
12		¹ D ₂ ^a	1.0250	1.0685	1.0262	1.2685
13		³ F ₂	1.1291	1.1691	1.1314	1.1304
14		³ F ₃	1.1390	1.1795	1.1424	1.1419
15		³ F ₄	1.1543	1.1962	1.1602	1.1610
16		¹ P ₁	1.2586	1.3019	1.3215	1.2479
17		³ P ₂	1.2984	1.3365	1.3042	1.3004
18		³ P ₁	1.3067	1.3453	1.3310	1.3009
19		³ P ₀	1.3156	1.3559	1.3283	1.2941
20		³ D ₁	1.3292	1.3673	1.3054	1.2816
21		³ D ₃	1.3331	1.3701	1.3255	1.2969
22		³ D ₂	1.3338	1.3718	1.3328	1.2704

Table 3. Continued.

23		¹ F ₃	1.4080	1.4427	1.3855	1.3548
24	4s 4p ³	¹ D ₂ ^a	1.4366	1.4801	1.4289	1.0258
I.P.	2.2322	2.2591	2.2585	2.2653
Se ³⁺						
Index	Config.	Term	Small	Medium	Large	NIST
1	4s ² 4p	² P _{1/2}	0.0000	0.0000	0.0000	0.0000
2		² P _{3/2}	0.0359	0.0408	0.0399	0.0399
3	4s 4p ²	⁴ P _{1/2}	0.6690	0.6954	0.7242	0.7235
4		⁴ P _{3/2}	0.6826	0.7110	0.7394	0.7379
5		⁴ P _{5/2}	0.7025	0.7332	0.7612	0.7617
6		² D _{3/2}	0.9631	0.9645	0.9848	0.9496
7		² D _{5/2}	0.9649	0.9675	0.9878	0.9542
8		² S _{1/2}	1.2240	1.2380	1.2570	1.1736
9		² P _{1/2}	1.3662	1.3312	1.3517	1.2405
10		² P _{3/2}	1.3883	1.3537	1.3735	1.2608
11	4s ² 4d	² D _{3/2}	1.4846	1.4520	1.4404	1.3962
12		² D _{5/2}	1.4868	1.4542	1.4425	1.3998
13	4p ³	² D _{3/2}	1.7948	1.8299	1.8413	1.7288
14		² D _{5/2}	1.7999	1.8360	1.8473	1.7948
16		² P _{3/2}	2.0512	2.0962	2.0974	1.9987
17		² P _{1/2}	2.0536	2.0988	2.0977	2.0644
I.P.	3.0904	3.1181	3.1140	3.1564
Se ⁴⁺						
Index	Config.	Term	Small	Medium	Large	NIST
1	4s ²	¹ S ₀	0.0000	0.0000	0.0000	0.0000
2	4s 4p	³ P ₀	0.7789	0.7712	0.8130	0.8179
3		³ P ₁	0.7912	0.7859	0.8255	0.8325
4		³ P ₂	0.8179	0.8188	0.8529	0.8654
5		¹ P ₁	1.2842	1.2353	1.2567	1.2004
6	4p ²	¹ D ₂	2.0516	1.8880	1.9396	1.9428
7		³ P ₀	1.8912	1.9003	1.9485	1.9300
8		³ P ₁	1.9072	1.9207	1.9655	1.9509
9		³ P ₂	1.9303	1.9585	1.9973	1.9922
10	4s 4d	³ D ₁	...	2.2974	2.3557	2.3468
11		³ D ₂	...	2.2996	2.3577	2.3488
12		³ D ₃	...	2.3029	2.3608	2.3518
I.P.	4.8651	4.8835	4.9191	5.0211
Se ⁵⁺						
Index	Config.	Term	Small	Medium	Large	NIST
1	4s	² S _{1/2}	0.0000	0.0000	0.0000	0.0000
2	4p	² P _{1/2}	1.0065	1.0063	1.0272	1.0276
3		² P _{3/2}	1.0521	1.0520	1.0840	1.0795
4	4d	² D _{3/2}	...	2.5111	2.5749	2.5773
5		² D _{5/2}	...	2.5168	2.5826	2.5835
I.P.	5.8878	5.8863	5.9592	6.0052
Se ⁶⁺						
Index	Config.	Term	Small	Medium	Large	NIST
1	3d ¹⁰	¹ S ₀	0.0000	0.0000	0.0000	0.0000
2	3d ⁹ 4s	³ D ₃	4.0123	4.0164	4.0173	4.0073
3		³ D ₂	4.0351	4.0393	4.0401	4.0289
4		³ D ₁	4.0731	4.0772	4.0781	4.0712
5		¹ D ₂	4.1138	4.1179	4.1187	4.1035
6	3d ⁹ 4p	³ P ₂	5.0873	5.0914	5.0929	5.0913
7		³ F ₃	5.1359	5.1400	5.1415	5.1360
8		³ P ₁	5.1468	5.1509	5.1524	5.1545
9		³ F ₄	5.1720	5.1762	5.1777	5.1771
10		³ F ₂	5.1760	5.1801	5.1816	5.1809
11		³ P ₀	5.1813	5.1854	5.1869	5.1922
12		¹ D ₂	5.2463	5.2505	5.2520	5.2408
13		¹ F ₃	5.2465	5.2507	5.2522	5.2448
14		³ D ₃	5.2703	5.2745	5.2760	5.2705
15		¹ P ₁	5.2816	5.2858	5.2873	5.2696
16		³ D ₁	5.3055	5.3098	5.3113	5.2989
17		³ D ₂	5.3128	5.3170	5.3185	5.3104
I.P. ^b	11.4209

^a The internal identification scheme within AUTOSTRUCTURE likely mislabeled the Se²⁺ 4s² 4p 4d and 4s 4p³ ¹D₂ terms, leading to the large discrepancies in calculated vs. experimental energies. If the identifications are exchanged, the energy agreement improves significantly.

^b Since we did not compute the electronic structure of Se⁷⁺, it was not possible to calculate the ionization potential of Se⁶⁺.

Table 4. Calculated Einstein A-coefficients (in s⁻¹) compared to literature values. A number in parentheses indicates a power of ten (i.e., 5.0(-10) = 5.0×10⁻¹⁰).

Se ⁰					
<i>i</i>	<i>j</i>	Small	Medium	Large	Previous ^a
1	2	1.50(-1)	1.64(-1)	1.64(-1)	1.71(-1)
1	3	1.53(-4)	4.53(-4)	4.29(-4)	1.96(-4)
2	3	9.28(-3)	7.38(-3)	8.58(-3)	1.03(-3)
1	4	7.59(-1)	7.84(-1)	7.97(-1)	6.40(-1)
2	4	1.50(-1)	1.47(-1)	1.51(-1)	1.08(-1)
3	4	5.71(-4)	6.25(-4)	5.28(-4)	7.86(-5)
1	5	4.50(-2)	1.26(-2)	2.46(-2)	1.89(-1)
2	5	6.83	6.88	7.26	7.61
4	5	5.26(-1)	5.47(-1)	8.44(-1)	2.44
1	6	...	7.41(5)	7.57(5)	1.70(6)
2	6	...	1.36(5)	1.44(5)	3.24(5)
1	7	...	7.92(8)	7.92(9)	2.13(8)
2	7	...	4.00(8)	4.01(8)	9.79(7)
3	7	...	1.30(8)	1.31(8)	3.30(7)
1	19	...	4.42(5)	1.26(7)	1.32(8)
1	20	...	9.38(6)	1.30(8)	1.46(7)
1	21	...	1.69(8)	6.61(8)	5.28(8)
Se ⁺					
<i>i</i>	<i>j</i>	Small	Medium	Large	Previous ^a
1	2	3.21(-1)	2.72(-1)	1.97(-1)	3.50(-1)
1	3	2.33(-2)	2.32(-2)	1.84(-2)	1.88(-2)
2	3	2.13(-3)	1.66(-3)	1.10(-3)	2.78(-3)
1	4	1.61	1.63	1.24	2.30
2	4	5.87(-1)	7.10(-1)	5.31(-1)	1.23
3	4	2.30(-2)	5.09(-2)	4.00(-2)	9.37(-2)
1	5	3.54	3.64	2.78	4.95
2	5	1.10	1.24	9.13(-1)	2.24
3	5	5.67(-1)	6.98(-1)	5.22(-1)	1.25
4	5	2.67(-3)	2.32(-3)	1.57(-3)	4.91(-3)
1	9	...	1.37(9)	1.52(9)	9.96(8)
1	10	...	1.41(9)	1.56(9)	1.03(9)
1	11	...	1.50(9)	1.65(9)	1.14(9)
Se ²⁺					
<i>i</i>	<i>j</i>	Small	Medium	Large	Previous ^a
1	2	5.72(-2)	6.75(-2)	9.19(-2)	9.59(-2)
1	3	9.63(-5)	1.15(-4)	1.84(-4)	1.66(-4)
2	3	1.03(-1)	1.23(-1)	1.48(-1)	1.35(-1)
1	4	1.81(-3)	1.36(-3)	2.27(-3)	2.37(-4)
2	4	6.21(-1)	7.34(-1)	8.70(-1)	8.00(-1)
3	4	1.15	1.32	1.50	1.21
2	5	1.22(1)	1.57(1)	1.69(1)	1.70(1)
3	5	1.42(-1)	3.38(-1)	3.62(-1)	5.81(-1)
4	5	7.46(-1)	2.17	1.57	2.81
Se ³⁺					
<i>i</i>	<i>j</i>	Small	Medium	Large	Previous ^a
1	2	5.51(-1)	8.06(-1)	7.57(-1)	7.58(-1)
1	6	2.78(8)	2.39(8)	2.66(8)	2.79(8)
2	6	2.06(7)	1.14(7)	1.33(7)	4.90(7)
2	7	2.62(8)	2.14(8)	2.41(8)	2.98(8)
Se ⁴⁺					
<i>i</i>	<i>j</i>	Small	Medium	Large	Previous ^a
1	3	2.30(6)	4.14(6)	4.13(6)	1.24(7)
1	5	8.04(9)	7.23(9)	8.50(9)	1.79(10)
Se ⁵⁺					
<i>i</i>	<i>j</i>	Small	Medium	Large	Previous ^a
1	2	2.31(9)	2.31(9)	2.56(9)	2.22(9)
1	3	2.64(9)	2.64(9)	3.01(9)	5.07(9)
2	4	...	9.67(9)	1.05(10)	1.95(10)
3	4	...	1.76(9)	1.88(9)	1.80(9)
3	5	...	1.07(10)	1.14(10)	1.64(10)

^a References for forbidden transitions in the ground configuration: Se⁰ (Biémont & Hansen 1986a), Se⁺ and Se²⁺ (Biémont & Hansen 1986b), Se³⁺ (Biémont & Hansen 1987). Morton (2000) is the reference for Se⁰–Se³⁺ permitted transitions, while those for Se⁴⁺ and Se⁵⁺ are taken from Migdalek & Stanek (1989), Bahr et al. (1982), and Curtis & Theodosiou (1989). To our knowledge, tabulated Se⁶⁺ Einstein A-coefficients have not been published.